| 1 | Using tracer observations to reduce the uncertainty of ocean diapycnal mixing and climate | | | | | | |
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| 2 | - carbon cycle projections | | | | | | |
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Abstract

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What is the uncertainty of climate-carbon cycle projections in response to anthropogenic greenhouse gas emissions and how can we reduce this uncertainty? We address this question by quantifying the ability of available ocean tracer observations to constrain the values of diapycnal diffusivity in the pelagic ocean (K_v) , a key uncertain parameter representing sub-gridscale diapycnal (vertical) mixing in physical circulation models. We show that model versions with weak mixing (i.e., low K_{ν}) lead to higher projections of atmospheric CO₂ and larger global warming than models with vigorous mixing. Slower heat uptake as well as slower carbon uptake by the oceans contribute about equally to the accelerated warming in the low mixing models. A Bayesian data-model fusion method is developed to quantify the likelihood of different structural and parametric model choices given an array of observed 20th century ocean tracer distributions. These spatially resolved observations provide strong limits on the upper value of K_{ν} , whereas global metrics used in previous studies—such as the historical evolution of global average surface air temperature, global ocean heat uptake, or atmospheric CO₂ concentration—provide only poor constraints. We compare different methods to quantify the probability of a particular diffusivity value given the observational constraints. One-dimensional, globally horizontally averaged data result in sharper probability density functions compared with the full 3D fields. This perhaps unexpected result opens up an avenue to objectively determine the optimal degree of aggregation at which model predictions have skill, and at which observations are most helpful in constraining model parameters. Our best estimate for K_v in the pelagic pycnocline is around 0.05-0.2 cm²/s, in agreement with earlier independent estimates based on tracer dispersion experiments and turbulence microstructure measurements.

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1. Introduction

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49 Atmospheric CO₂ concentrations are rising faster than ever since continuous monitoring began in 50 1959 [Canadell et al., 2007]. Increasing anthropogenic carbon emissions is the main cause of 51 this accelerating growth, but reduced uptake of atmospheric CO₂ by ocean [Le Quere et al., 52 2007] and land are also hypothesized to play a role [Canadell et al., 2007]. These observations 53 are consistent with previous coupled climate-carbon cycle model simulations that predict 54 decreases in terrestrial and oceanic carbon uptake in the future due to changes in climate [Cox et 55 al., 2000; Dufresne et al., 2002; Friedlingstein et al., 2006; Govindasamy et al., 2005; Jones et 56 al., 2003; Joos et al., 1999; Joos et al., 2001; Matear and Hirst, 1999; Matthews et al., 2005b; 57 Sarmiento et al., 1998; Zeng et al., 2004]. However, the Coupled Climate - Carbon Cycle Model Intercomparison Project (C⁴MIP) [Friedlingstein et al., 2006] shows a large range in the 58 59 projected magnitude of this feedback between different models. Projected atmospheric CO₂ 60 levels for emission scenario SRES A2 at year 2100 range from ~700 ppmv to ~1000 ppmv, and 61 up to 200 ppmv of this difference can be attributed to differences in the climate-carbon cycle 62 feedback [Friedlingstein et al., 2006]. Thus, the unknown magnitude and uncertainty of the 63 future climate-carbon cycle feedback presents a major hindrance in the assessment of the impacts 64 of carbon emission scenarios. 65 66 The reasons for the aforementioned model differences are poorly understood. Although the 67 C⁴MIP models showed larger differences in land uptake (-6 to +10 GtC/yr), there were also 68 considerable differences in ocean uptake (+4 to +10 GtC/yr) by the year 2100 [Friedlingstein et 69 al., 2006]. Matthews et al. [2005a] shows that differences in the parameterizations of the 70 dependency of terrestrial vegetation growth rates on ambient temperatures have a large effect on 71 carbon uptake on land in future warming experiments, suggesting that this might be a major contributor to the uncertainty range observed in the C⁴MIP models. Even less is known about 72 73 reasons for the differences in ocean uptake, although more simplified models (either in terms of 74 physics or biology) apparently show a larger sensitivity of carbon uptake with respect to 75 temperature changes than more complex models [Friedlingstein et al., 2006]. A more detailed 76 comparison between two specific models attributes a two fold difference in oceanic carbon 77 uptake (4 GtC/yr in the UK Hadley Center model versus 8 GtC/yr in the French IPSL model at

78 700 ppmy atmospheric CO₂) due to increasing CO₂ alone (without climate change) to differences 79 in Southern Ocean circulation [Friedlingstein et al., 2003]. 80 The models included in the C⁴MIP exercise are very heterogeneous and range from box models 81 82 to zonally averaged and slab mixed layer ocean models to fully three-dimensional coupled 83 atmosphere-ocean general circulation models (AOGCMs). These studies are mostly silent on the 84 question of how probable the different model structures are given the available observational 85 constraints. Without a systematic and probabilistic comparison between observations and the 86 C⁴MIP models, it remains unclear how to interpret the range covered by the C⁴MIP models. A 87 careful probabilistic analysis of whether the models are consistent with observations can provide 88 important insights into this question [Doney et al., 2004; Matsumoto et al., 2004]. 89 90 It is also likely that the C⁴MIP model simulations do not cover the full scope of uncertainty in 91 possible future climate-carbon interactions, due to (for example) an incomplete representation of 92 the range of unconstrained parameters. Recent Monte Carlo simulations with an atmosphere 93 model suggest that model parameter uncertainties can increase the range of future climate 94 projections considerably [Murphy et al., 2004; Stainforth et al., 2005]. A key uncertain 95 parameter in ocean circulation models is the diapycnal (vertical) diffusivity K_{ν} . The strong 96 sensitivity of the global deep overturning circulation to K_{ν} has been known since the pioneering 97 study by Bryan [1987]. Here we investigate the uncertainty in ocean vertical mixing and its 98 effect on future projections of climate and CO₂. 99 100 Earlier studies show that tracer distributions in ocean models are sensitive to changes in ocean 101 circulation and ventilation [Doney et al., 2004; England and Maier-Reimer, 2001; Gnanadesikan 102 et al., 2004; Matsumoto et al., 2004], but no attempt has been undertaken to quantify the 103 probability of different model structures and parameters given spatially resolved observations of 104 ocean tracer distributions. Probabilistic approaches to climate projections have only been 105 developed in recent years. These pioneering studies were designed to estimate the probability 106 density function (PDF) of the climate sensitivity and used simple model structures constrained 107 only by globally aggregated observations such as the global mean surface air temperature 108 evolution since 1850 [Andronova and Schlesinger, 2001], global mean ocean heat content

109 changes [Forest et al., 2002; Knutti et al., 2003; Tomassini et al., 2007], atmospheric CO₂ 110 [Ricciuto et al., 2008], global carbon emissions [Jones et al., 2006], or paleoclimate data [Annan 111 et al., 2005; Schneider von Deimling et al., 2006]. Tomassini et al. [2007] found a multimodal 112 probability distribution for K_{ν} , and concluded that these globally averaged metrics do not provide 113 strong limits on the value of K_{ν} . Here we show that multiple physical, geochemical and 114 biogeochemical observations with spatial resolution can provide much stronger constraints on 115 the diapycnal ocean diffusivity. The main goal of this paper, however, is to develop and 116 demonstrate a Bayesian data-model fusion approach for spatially distributed tracer observations

that can be used to assess and reduce the uncertainty of future climate projections.

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2. Methods

2.1. Model

The UVic Earth System Climate Model [Weaver et al., 2001] of intermediate complexity, includes a coarse resolution (1.8x3.6°, 19 vertical layers) three-dimensional general circulation model of the ocean. It has state-of-the-art physical parameterizations such as diffusive mixing along and across isopycnals, eddy induced tracer advection [Gent and McWilliams, 1990] and a scheme for the computation of tidally induced diapycnal mixing over rough topography [Simmons et al., 2004]. In order to account for other sources of mixing, a globally constant background diffusivity K_{bg} is added to the tidally induced diffusivity $K_v = K_{tidal} + K_{bg}$. It is unlikely that breaking of internal waves and other unconsidered sources of mixing are spatially constant, but lacking process based parameterizations, K_{bg} is assumed constant within the current model context. It is this background diffusivity K_{bg} that we vary in our sensitivity study, from 0.01 cm²/s to 0.5 cm²/s. The tidally induced diffusivity rapidly decays in the water column above the sea floor with an exponential depth scale of 500 m. This results in the background diffusivity determining the value of diapycnal mixing in most parts of the pelagic pycnocline. Observations from the Southern Ocean show that diapycnal mixing is much larger than in other oceans [Naveira Garabato et al., 2004]. We account for these observations by limiting K_v to ≥ 1 cm²/s south of 40°S. Thus, the variations in K_{bg} affect mixing only in the open ocean north of 40°S.

138 A simple one-layer atmospheric energy-moisture balance model (EMBM) interactively 139 calculates heat and water fluxes to ocean, land and sea ice, while wind velocities are prescribed 140 from the NCAR/NCEP monthly climatology in the momentum transfer to the ocean and to a 141 dynamic-thermodynamic sea ice model. The model does not use flux corrections. The model of 142 the terrestrial vegetation and carbon cycle [Meissner et al., 2003] is based on the Hadley Center 143 model TRIFFID. The ocean biogeochemical model is based on the NPZD (nutrient, 144 phytoplankton, zooplankton, detritus) ecosystem model of Schmittner et al. [2005b], and 145 includes a parameterization of fast nutrient recycling due to microbial activity after Schartau and 146 Oschlies [2003]. It solves prognostic equations for two phytoplankton classes (nitrogen fixers 147 and other phytoplankton) as well as for nitrate, phosphate, oxygen, dissolved inorganic carbon, 148 alkalinity, radiocarbon and chlorofluorocarbons as tracers. The biogeochemical/carbon cycle 149 model is described in detail in Schmittner et al. [2008]. Biological uptake and release occurs in 150 fixed elemental ratios of carbon, phosphate, nitrate and oxygen. Calcium carbonate production is 151 parameterized as a fixed ratio of the production of particulate organic matter in the water 152 column. Remineralization of calcium carbonate is determined by instantaneous sinking with an 153 e-folding depth of 3500 m. 154 The ensemble consists of 8 models with K_{bg} =(0.01,0.05,0.1,0.15,0.2,0.3,0.4,0.5). (In the 155 following, for brevity, we omit the units of K_{bg} , which are in cm²/s.) Each model version is 156 157 restarted from an 8000 year control integration with K_{bg} =0.15, and spun up for an additional 3000-4000 years (longer for smaller K_{bg}) using constant pre-industrial forcing until climate and 158 159 carbon cycle are in quasi-equilibrium. Initially atmospheric CO₂ is fixed at 280 ppmv, but for the 160 last ~1000 years of the spin up it is calculated interactively. Equilibrium is determined if changes 161 in atmospheric CO₂ are less than 5 ppmv per 1000 years, so that at the end of the spin up 162 atmospheric CO₂ is within ±5 ppmv of ice core measurements of its pre-industrial value of 280 163 ppmy (Figure 1) for all model versions. Subsequent estimates [Crowley, 2000] of historical 164 forcing from year 1800 to 1998 AD are applied, considering changes in solar insolation, volcanic 165 and anthropogenic aerosol and greenhouse gases, followed by CO₂ emission scenario SRES A2 until 2100 and a linear decrease of emissions to zero from year 2100 to 2300 (Figure 1). Solar, 166 167 aerosol and non-CO₂ greenhouse gas forcings have been held constant at 1988-1998 levels for 168 the future simulations.

169 170 2.2. Observations 171 We calculate probability densities for nine three-dimensional tracer distributions from two 172 databases. Temperature (T) [Locarnini et al., 2006], salinity (S) [Antonov et al., 2006], phosphate 173 (PO₄) [Garcia et al., 2006a], apparent oxygen utilization (AOU) [Garcia et al., 2006b] and 174 preformed phosphate ($P^*=PO_4$ -AOU/170) are taken from the World Ocean Atlas 2005 (WOA05, data downloaded from ftp.nodc.noaa.gov/pub/data.nodc/woa/WOA05nc) and radiocarbon 175 $(\Delta^{14}C)$, chlorofluorocarbon 11 (CFC11), dissolved inorganic carbon (DIC), and alkalinity (ALK) 176 177 are adopted from the Global Ocean Data Analysis Project (GLODAP) [Key et al., 2004]. Both 178 databases provide data on a 1×1° grid with 33 vertical levels. The observations are averaged 179 onto the 1.8×3.6° model grid with 19 vertical levels. GLODAP data represent the 1990s and are 180 compared with the decadal model mean from 1990-2000, whereas WOA05 data represent the 181 1950-2000 and are compared to the model mean during this period. 182 183 2.3. Observation Error Estimates 184 To quantitatively compare observations to model projections requires an estimate of the 185 observation errors. The error size determines how far from the data a model can be and still 186 remain consistent with the observations. Spatially variable error estimates for the observations (σ_{Oi}) are available for $\Delta^{14}C$, CFC, DIC and ALK from the GLODAP data set representing errors 187 188 resulting from the objective analysis (mapping) procedure used to interpolate and extrapolate 189 observations to a global grid. Due to the sparse observations the GLODAP error estimates are 190 horizontally correlated with a correlation length scale of 10-20°. Thus the GLODAP errors are 191 simply averaged onto the model grid. 192 193 The WOA05 provides the standard error for each unanalyzed variable, which is the standard 194 deviation of the mean divided by the square root of the number of observations in each grid cell. 195 Following the recommendation in the WOA05 documentation (available at

http://www.nodc.noaa.gov/OC5/WOA05/pr woa05.html) the error due to the objective analysis

is estimated as the difference between the value of the analyzed field and the mean at each grid

cell containing observations. For T and S, which have observations at almost all grid points, this

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error is horizontally uncorrelated. The global horizontal root mean square is calculated at each depth level, representing the (horizontally uniform but vertically varying) mapping error. This mapping error is added to the standard error to yield the spatially variable total error estimate.

For PO_4 , pre-formed PO_4 , and AOU the data density is too sparse to calculate an error estimate due to the mapping procedure, because the calculation outlined above can only be performed for points that include data. For this reason we do not use the analyzed fields but rather we use the unanalyzed mean (the average of the raw observations in any given $1x1^{\circ}$ data grid box). This limits the number of grid cells to those containing observations. The observations are averaged onto the model grid, and model grid cells without observations are discarded in the analysis. In this case the total error of the observations is only the standard error of the mean (no mapping error). For all WOA05 variables the total errors are assumed to be horizontally uncorrelated and are hence averaged onto the model grid and divided by $2.55 = \sqrt{3.6 \times 1.8}$ in order to account for 6.48 independent data grid boxes in one model grid cell.

2.4. Statistical Analysis

We assess the compatibility of different diapycnal diffusivities with observed tracer measurements using Bayesian inference to compute the relative probability of each of the eight diffusivities in our ensemble implied by each of the nine tracer fields. Two different methods are used in the model assessment. The first computes the root mean squared (RMS) error (E) for each model, including the full three-dimensional (3D) spatial fields of observations. This method neglects the correlation of the errors and requires the size of the errors to be specified. The second method considers the correlation of the errors and determines the error magnitude and bias endogeneously from the data-model residuals. However, due to computational constraints it uses only 1-dimensional data (globally horizontally averaged depth profiles). Both methods, as well as the relations between them, are described in detail below.

2.4.1. The 3D Method

Models that greatly differ from the observations are judged less probable than models whose deviations from the data are small. To quantify this intuition, it is necessary to mathematically

specify what "small" means. We introduce an error estimate σ to set the scale against which data-model discrepancies are evaluated. These deviations are deemed large or small relative to the magnitude of σ . Observations can differ from model predictions for two reasons: model structural error, and observational/measurement error. The quality of data-model agreement depends on how large we judge these errors to be (see Sec. 3.7). However, errors can be difficult to estimate *a priori* (before seeing the observational data), especially when model structural errors are substantial. Observational errors usually can be estimated from known properties of the measurement system (Sec. 2.3), but the size of the model error typically cannot be determined without comparing the model output to observations.

To assess model skill for each tracer i, we calculate the error-weighted mean squared error

$$\overline{E_i^2} = \overline{\left(\frac{O_i - M_i}{\sigma_i}\right)^2} \,. \tag{1}$$

The overbar denotes the global, volume-weighted average. Deviations of each modeled 3D tracer field $M_i = M_i(x,y,z) = \overline{M_i} + M_i'$ from the observations $O_i = O_i(x,y,z) = \overline{O_i} + O_i'$ are weighted by a combined error estimate $(\sigma_i^2 = \sigma_{Oi}^2 + \sigma_{Mi}^2)$ for the observations σ_{Oi} and the model σ_{Mi} . (The prime denotes the deviation from the global mean.) Our methods for estimating the observation and model errors are discussed in Section 3.4.1.

The models often show bias relative to the observations, so that their mean prediction differs from the mean of the observations. To distinguish between the amount of error introduced by model bias and the amount of error unrelated to bias, we also consider the bias-corrected RMS error. This error is calculated by subtracting the global mean bias $b_i = \overline{O_i} - \overline{M_i}$, so that the bias corrected residuals $O_i - M_i - b_i$ have zero mean. The bias-corrected RMS error is then

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$$\overline{E_i'^2} = \overline{\left(\frac{O_i - M_i - b_i}{\sigma_i}\right)^2} = \overline{\left(\frac{O_i' - M_i'}{\sigma_i}\right)^2}$$
. The error $\overline{E_i'^2}$ excludes information about the global mean

255 data-model misfit.

The probabilistic model assessment, however, includes information on the global mean datamodel misfit using equation (1). Assuming the errors are independent and identically-distributed random variables, the probability density

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$$L(O_i \mid K_{bg}) \propto \exp(-\frac{1}{2}E_i^2)$$
 (2)

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- is the likelihood that the observations O_i could arise from the model with parameter K_{bg} . Above,
- 263 $E_i^2 = \overline{E_i^2} \times N$ is the (volume-weighted, error-weighted) sum of squared errors, equal to the mean
- squared error $\overline{E_i}^2$ times the number of data points (N). More precisely, assuming a known error
- o, the probability in equation (2) is a normal likelihood function: the observations are assumed to
- be drawn from a normal distribution with mean centered on the model output
- $(O \sim N(\mu = M, \sigma^2))$. Bayes' theorem states that the posterior probability density function (PDF)
- for K_{bg} is proportional to the product of the likelihood of the observations with the prior PDF of
- 269 K_{bg} , p(K_{bg}):

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$$p(K_{be}|O_i) \propto L(O_i|K_{be}) \times p(K_{be}) . \tag{3}$$

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- The prior PDF quantifies expert judgment about the value of K_{bg} before having assimilated the
- observational data. We adopt a uniform prior PDF for K_{bg} , giving equal prior probability to
- each model run. The posterior probability of a particular model run is the product of how likely
- 276 the data are given the model output, weighted by how probable the run is judged to be *a priori*.
- See Gelman et al. {, 2004 #424} for a basic reference text on Bayesian methods.

- 279 If the errors in different tracers are independent of each other which is generally *not* the case,
- as discussed below likelihoods for individual tracers can be multiplied to yield the combined
- likelihood of all tracers, $L(O \mid K_{bg}) = \prod_{i} L(O_i \mid K_{bg})$. Probability-weighted projections for a
- climate variable T are obtained by averaging over the possible values of K_{bg} ,

$$\overline{T} = \int_{Kbemin}^{Kbgmax} T(K_{bg}) \cdot p(K_{bg} \mid O) dK_{bg}, \qquad (4)$$

if the PDF is defined on the interval [K_{bgmin} , K_{bgmax}].

2.4.2. The 1D Method

The above 3D method ignores spatial autocorrelation of the data-model residuals, $R_i = O_i - M_i$, which is known to lead to overconfident parameter estimates [*Zellner and Tiao*, 1964]. In addition, the above formulation presumes that the residual error σ is known, but as discussed in the previous section, it can be difficult to estimate *a priori*. Here we develop a relatively simple and computationally efficient method to estimate the combined effects of observation errors and model structural errors endogenously from the overall data-model misfit. This method is more computationally expensive than the 3D method, so we apply it to small 1D aggregated data sets instead of to the full 3D spatial fields.

When the errors are uncorrelated, only their magnitudes σ_i need to be specified. If the errors are correlated, the correlation between errors must be specified in addition to their magnitudes. We generalize from the error variances σ_i^2 to an error covariance matrix Σ , which includes the error variances and the spatial correlations between points. In the 3D method we use the weighted sum of squared errors, $\sum_i (O_i - M_i)^2 / \sigma_i^2$, to quantify model skill. This error measure is not appropriate when the errors are correlated. Correlated errors effectively provide fewer independent data points than uncorrelated errors. An appropriate measure should penalize models less harshly when correlation is present, since fewer independent data are assimilated. To include correlation the sum of squared errors generalizes to a quantity involving the error covariance matrix, known as the Mahalanobis distance [*Mahalanobis*, 1936], which appears in the multivariate normal distribution:

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$$E_i^2 = (O_i - M_i)^T \Sigma_i^{-1} (O_i - M_i).$$
 (5)

This expression reduces to the sum of squared errors when the covariance matrix is diagonal with entries σ_i^2 , i.e., when it contains only variances but no off-diagonal correlations. (In the remainder of this section we omit the subscript *i* when referring to each tracer.)

Only small covariance matrices are used here because matrix inversion is computationally expensive, growing with the cube of the number of data points. To reduce the size of the covariance matrix to a computationally feasible magnitude, we consider only a 1D globally averaged spatial field of tracer data O(z) and M(z) as a function of depth z. Each field is reduced to 18 data points (depths), allowing the assimilation to run for all tracers within a few minutes on a single workstation. A small 2D latitude-depth grid may also be computationally feasible to assimilate in this manner, but this exercise is beyond the scope of this proof-of-concept study. We assume the covariance matrix Σ is given by a stationary squared-exponential covariance function between depths z_j and z_k , $\Sigma_{jk} = \sigma^2 \exp(-|z_j - z_k|^2/\lambda^2)$, where σ^2 is the residual variance and λ is a range or correlation length parameter. A squared-exponential covariance function implies a smooth (infinitely differentiable) spatial process, and is chosen because prior judgment as well as inspection of the residuals suggest that the globally-averaged model structural error varies smoothly with depth. Including the possibility of a constant model bias, b, the observations are assumed to be drawn from a multivariate normal likelihood centered on the bias-corrected model output ($O \sim MVN(\mu = M + b, \Sigma)$).

In the previously discussed 3D method, the residual error σ , the correlation length λ , and the model bias b are assumed known constants (with λ =0, and b=0 or set to the difference in observational and model means). These constants may differ between tracers. In the 1D method applied here, we relax these assumptions by treating the three constants as unknown statistical parameters. The full Bayesian approach, which we approximate, is to calculate a joint posterior PDF for all the uncertain parameters, including the model parameter K_{bg} and the three statistical parameters. By Bayes' theorem, this posterior probability is proportional to the product of the likelihood of the observations with the prior probability of the parameters,

$$p(K_{bg}, \sigma, \lambda, b|O) \propto L(O|K_{bg}, \sigma, \lambda, b) \times p(K_{bg}, \sigma, \lambda, b).$$
 (6)

We are most interested in the probabilities of the different model diffusivities, not of the statistical parameters. We can obtain the posterior PDF $p(K_{bg}|O)$ for K_{bg} alone by integrating the joint posterior $p(K_{bg},\sigma,\lambda,b|O)$, Eq. 6, with respect to the three statistical parameters:

$$p(K_{bg} \mid O) = \iiint p(K_{bg}, \sigma, \lambda, b \mid O) \, d\sigma d\lambda db.$$

$$348 (7)$$

However, for computational simplicity, we avoid performing this integral by fixing the statistical parameters at their best-fit values σ^* , λ^* , β^* . This gives an approximate proportionality

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$$p(K_{bg} \mid O) \approx p(K_{bg} \mid O, \sigma^*, \lambda^*, b^*) \propto L(O \mid K_{bg}, \sigma^*, \lambda^*, b^*) \times p(K_{bg}, \sigma^*, \lambda^*, b^*). \tag{8}$$

Fixing the statistical parameters ignores their uncertainty but still accounts for the presence of model error, bias, and correlation. These quantities are estimated from the data-model misfit instead of assumed from expert prior judgment. The best estimate for σ^* , λ^* , β^* is obtained by numerically maximizing the posterior probability (Eq. 6) using a global optimization method [Storn and Price, 1997] to account for potential multimodality. Posterior maximization is analogous to maximum likelihood estimation [Lehmann and Casella, 2003], except that the likelihood is modified by prior constraints on the parameters. The statistical parameters are separately optimized for each tracer, allowing the estimated residual structure to vary between tracers. For every tracer, the parameters are also re-optimized for each member of the ensemble. In other words, the statistical parameters are allowed to depend on K_{bg} . The logic behind this assumption is that the model error depends on the model parameters, since poorly fitting models should have larger model error and bias. We linearly interpolate the posterior probability onto a regular grid of K_{bg} and normalize the integral to unity to arrive at a proper probability density function.

We choose a uniform prior for the model parameter K_{bg} . The correlation length prior is $p(\lambda)=Lognormal(5.5,0.5^2)$. That is, $ln(\lambda)$ is normally distributed with a mean 5.5 and standard

deviation 0.5, which puts most of its probability mass between 0 and 600 meters and practically excludes larger correlation lengths. Large correlation lengths imply strong communication between the surface and the deep ocean, which is contrary to the layered nature and highly stratified vertical structure of the ocean. We use a joint prior for the residual variance and bias, $p(b/\sigma) = N(0,0.5^2)$. This prior is selected so the model bias for the best K_{bg} value is assumed to be likely smaller than the residual error (i.e., b/σ is near zero). This gives low prior weight to models with large biases, where "large" is quantified relative to the size of the bias-corrected error, σ . Exploratory analysis indicates that an improper, unbounded uniform prior for the range or bias parameters can lead to ill-conditioned covariance matrices and non-robust results for the K_{bg} posterior distribution.

3. Results

3.1. Global Metrics

Observed atmospheric CO₂ concentrations and global mean surface air temperatures are simulated roughly equally well in all model versions, irrespective of the value of K_{bg} (Figure 1). This is also true for the ocean heat content changes, which are very similar in all simulations (Figure 2). As already concluded in *Tomassini et al.* [2007], these globally aggregated observations provide relatively poor constraints on K_{bg} . The model suggests, however, that this situation might change in the future, because the simulations for different K_{bg} values diverge notably during the 21st century. For example, at year 2100 differences in CO2 concentrations are about 70 ppmv (Figure 1). This suggests also that variations in diapycnal diffusivity alone can account for about 25% of the range in the C⁴MIP models. At year 2300 differences in CO₂ concentrations are more than 200 ppmv. Differences in projected global average surface air temperatures are 0.8°C in model year 2100 and 1°C in year 2300.

A 1°C variance with respect to a 7°C global warming might not seem significant compared to the much larger variance in the C⁴MIP or IPCC AR4 model projections. However, it is important to remember that the multi-model spread is caused by numerous differences in model structures and parameter values, whereas here we have only varied a single parameter.

402 3.2. Influence of Diapycnal Mixing on Climate-Carbon Cycle Projections 403 Larger diapycnal mixing leads to faster oceanic uptake of heat and CO₂ in the model. Both 404 effects tend to delay and reduce atmospheric warming. Faster CO₂ uptake leads to lower 405 atmospheric CO₂ concentrations and thus reduced radiative forcing, whereas faster heat uptake 406 leads to slower warming of surface waters and therefore delayed warming of surface air temperatures. We separate these two effects by comparing a simulation with weak mixing (K_{bg} = 407 408 0.1) forced with interactive CO₂ to one forced with a prescribed CO₂ evolution (and thus 409 radiative forcing) taken from a run with vigorous mixing ($K_{bg} = 0.5$). The difference in surface 410 air temperature evolution between these two simulations is due only to the effect of slower ocean 411 heat uptake. The effect of different ocean carbon uptakes is quantified by comparing the simulation with prescribed CO₂ to the fully coupled run with $K_{bg} = 0.1$ (Figure 3). The global 412 413 surface air temperature increase in the run with prescribed CO₂ evolution is about half way 414 between the experiments with high and low K_{bg} . About 55% (0.5 K) of the reduced warming of air temperatures in the high versus the low K_{bg} simulation is explained by differences in ocean 415 416 heat uptake alone, and 45% is caused by faster CO₂ uptake. This demonstrates that both effects, 417 slower heat uptake and slower carbon uptake, provide similar contributions to the reduced 418 warming in the high mixing model projections. 419 420 We analyze the sensitivity of land (ΔC_L) and ocean (ΔC_O) carbon uptake until year 2100 with 421 respect to changes in atmospheric CO₂ ($\beta_L = \Delta C^u_L/\Delta C^u_A$; $\beta_O = \Delta C^u_O/\Delta C^u_A$) and climate ($\gamma_L =$ $(\Delta C^c_L - \beta_L \Delta C^c_A)/\Delta T^c$; $\gamma_O = (\Delta C^c_O - \beta_O \Delta C^c_A)/\Delta T^c$) following Friedlingstein et al. [2006], where c and 422 423 u superscripts denote the coupled and uncoupled (constant climate) runs respectively, ΔT is the 424 global mean surface air temperature change and ΔC_A is the atmospheric CO₂ anomaly. As expected the land sensitivities $(\beta_L(K_{bg} = 0.1) = \beta_L(K_{bg} = 0.5) = 1.4 \text{ GtC/ppm}; \gamma_L(K_{bg} = 0.1) = -1.4 \text{ GtC/ppm}; \gamma_L(K_{bg} = 0.1$ 425 114 GtC/K; $\gamma_L(K_{bg} = 0.5) = -116$ GtC/K) are very similar between the different K_{bg} simulations. 426 (The C⁴MIP range for β_L is 0.2 to 2.8 GtC/ppm and for γ_L it is -20 to -177 GtC/K.) 427 428 429 However, ocean carbon uptake due to changes in atmospheric CO₂ alone is 30% smaller in the

low mixing model ($\beta_O(K_{bg} = 0.1) = 1$ CtC/ppm) compared to the high mixing model ($\beta_O(K_{bg} = 0.1) = 1$ CtC/ppm) compared to the high mixing model ($\beta_O(K_{bg} = 0.1) = 1$ CtC/ppm)

0.5) = 1.4 CtC/ppm). This suggests that differences in ocean diapycnal mixing alone can explain

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| 432 | half the range of β_O in the C ⁴ MIP models (0.8-1.6 GtC/ppm) and re-emphasizes the important |
|-----|---|
| 433 | role of diapycnal mixing on anthropogenic carbon uptake by the ocean. There are, of course, |
| 434 | other processes that additionally determine ocean carbon uptake (under fixed climate), such as |
| 435 | the strength of the overturning circulation and convection, mixed layer depths, and air-sea gas |
| 436 | exchange (driven by factors such as sea ice and wind velocities). |
| 437 | |
| 438 | Ocean carbon uptake decreases in the model simulations as climate warms due to increasing |
| 439 | stratification of the upper ocean. A greater weakening of the ocean carbon sink corresponds to |
| 440 | more negative values of γ_O . In the high mixing models this decrease is larger ($\gamma_O(K_{bg}=0.5)=-45$ |
| 441 | GtC/K) than in the low mixing models ($\gamma_O(K_{bg} = 0.1) = -31$ GtC/K). The C ⁴ MIP models range |
| 442 | from -14 to -67 GtC/K (though it is worth noting that the γ_O value of -67 GtC/K is the result of a |
| 443 | box model; the next largest C ⁴ MIP model value of γ_O is -46 GtC/K). At year 2100 the ocean |
| 444 | takes up 4.8 GtC/yr in the low mixing model versus 6.2 GtC/yr in the high mixing model. Most |
| 445 | (8 out of 11) C ⁴ MIP models lay within that range of ocean carbon uptake. |
| 446 | |
| 447 | The strength of positive climate-carbon cycle feedbacks can be quantified by the feedback gain |
| 448 | $(g = 1 - \Delta C^u_A/\Delta C^c_A = -\alpha(\gamma_L + \gamma_O)/(1 + \beta_L + \beta_O)$, where $\alpha = \Delta T^c/\Delta C^c_A$ is the transient climate |
| 449 | sensitivity) [Friedlingstein et al., 2006]. The effects of higher β_0 and larger (negative) γ_0 almost |
| 450 | completely compensate each other, but due to the larger transient climate sensitivity (α (K_{bg} = |
| 451 | 0.1) = 0.0060K/ppm versus α (K_{bg} = 0.5) = 0.0055K/ppm) there is a modest (10%) increase in |
| 452 | gain in the low mixing model ($g(K_{bg} = 0.1) = 0.2$) compared to the high mixing model ($g(K_{bg} = 0.1) = 0.2$) |
| 453 | 0.5) = 0.18). The range of g in the C ⁴ MIP models is 0.04-0.31, which includes differences in |
| 454 | both terrestrial and oceanic carbon cycle contributions to the total climate-carbon cycle feedback, |
| 455 | in addition to different values of transient climate sensitivity. According to our analysis, while |
| 456 | different K_{bg} values can explain a substantial portion of the range of ocean carbon uptake |
| 457 | between models, K_{bg} differences can explain only a relatively small proportion of the inter-model |
| 458 | range in net climate-carbon cycle feedback strength. |
| 459 | |

3.3. Model Assessment Using Spatially Resolved Ocean Tracer Observations

3.3.1. **Model and Observation Error Estimates**

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463 Assessing model skill requires an estimate of the discrepancy between observations and model 464 predictions. The 3D method's likelihood function, Equation (2), assumes that the standard 465 deviation of the data-model residuals (σ) is known. The 1D method estimates this error from 466 the residuals by an optimization procedure (Sec. 2.4.2). For the 3D method we choose to 467 determine the residual error by more informal means. By definition, the residual error $\sigma_i = \sqrt{\sigma_{Oi}^2 + \sigma_{Mi}^2}$ should be similar to the standard deviation of the residuals, $\sigma_i \approx SD(O_i - M_i)$. 468 469 For the 3D method we choose the model error σ_{Mi} such that this is the case for one of the best fitting models ($K_{bg} = 0.15$). (See Table 1 for values.) This model error is then applied to all 470 471 ensemble members. 472 473 The model error estimates σ_{Mi} can also be interpreted as measures of model quality; they can be 474 used for different models and are suitable for model intercomparisons. For example, for temperature and salinity, the values in the second row of Table 1 (3D data and $\sigma_0 = 0$) 475 476 correspond to the global RMS error. They can be compared to those reported for the OCMIP 477 models [Doney et al., 2004, Table 2] and a subset of the Intergovernmental Panel on Climate 478 Change Fourth Assessment Report (IPCC AR4) models [Schmittner et al., 2005a]. The OCMIP 479 range for 3D models without internal restoring is 0.84-2.18 K for temperature and 0.15-0.31 for 480 salinity; for the IPCC AR4 fully coupled ocean atmosphere models it is 0.86-2.97 K for 481 temperature and 0.20-0.38 for salinity. 482 483 We use the observational errors reviewed in Section 2.3 for the 3D method. For the 1D method 484 we assume that the observation error is negligible compared with the model error, since the global averaging leads to very small observational errors (decreasing with $\sim N_{eff}^{-1/2}$, where N_{eff} is 485 486 the effective number of observations). This is consistent with the 1D data-model residuals, which 487 show a smoothly varying structure more indicative of systematic model error than random 488 observation noise. 489 490 With these error estimates, we evaluate the skill of each of the eight models in the ensemble using three metrics. We use the root mean squared (RMS) error introduced in Section 2.4.1, as

well as the bias-corrected RMS error. We also compute the correlation between the observations and each model. A higher correlation indicates greater similarity between the model and the observations. We conduct sensitivity studies to explore how model skill varies with K_{ν} as determined by each of the three skill measures.

In the following discussion we distinguish between tracers which are influenced by physical processes only such as T, S, $\Delta^{14}C$, and CFC11, and those tracers strongly affected by biological processes such as PO_4 , AOU, P^* , DIC, and ALK, since the latter also depend on the choice of uncertain biological model parameters. Biological effects on the radiocarbon distribution in the ocean are about 2 orders of magnitude smaller than the physical effects of decay and air-sea gas exchange.

The RMS and bias-corrected RMS errors, E and E', are plotted in Figure 4 together with the correlation coefficients $r_i = \overline{M_i O_i} / \sqrt{\text{var}(M_i) \cdot \text{var}(O_i)}$, with the variance $\text{var}(x) = \overline{x^2} - \overline{x}^2$, using the full 3-dimensional data. The different tracers show different sensitivities to K_{bg} depending on the global metric considered. When measured by the RMS error E, the model skill for the $\Delta^{I4}C$, AOU, P^* and DIC tracers show the largest sensitivity to changes in K_v . Much of this sensitivity, however, is due to the model bias, as revealed by the difference between E and the bias corrected error E'. For S, ALK and PO_4 the bias is zero (E=E') because neither of these tracers exchanges with other climate system components in the model and hence their ocean inventories are fixed. When measured by the correlation coefficient, the model skill for the AOU and S tracers are most sensitive to variations in K_{bg} .

Most tracers are in better agreement with the observations for small values of K_{bg} , both for E and r as metrics. Correlation coefficients between model output and observations peak between 0.05 and 0.15 for all tracers except DIC and T, which are rather insensitive. AOU, DIC, $\Delta^{l4}C$ and P^* show very large biases for large values of K_{bg} . The deep ocean is much too young ($\Delta^{l4}C$ too high), too vigorously ventilated (AOU too low), too poor in inorganic carbon and too high in preformed nutrients. Even if the bias is removed, the bias-corrected RMS error E' in AOU is still much larger for the high K_{bg} models. CFC11 and S are both moderately sensitive and show better agreement with the observations for low K_{ν} , irrespective of the metric considered. PO_4 and ALK

523 are also moderately sensitive and show minima in RMS errors and maxima in correlation around 524 $K_{bg} = 0.15$. 525 526 3.4. Probabilities From the 3D Method PDFs from the 3D method suggest that $\Delta^{14}C$ is the most sensitive of the physical variables to 527 changes in K_v , followed by CFC11, T and S (Figure 5). $\Delta^{14}C$, S, and CFC11 show the maximum 528 probability for small values of K_{bg} . For $\Delta^{14}C$ the probability for small K_{bg} is about three times as 529 high as that for high K_{bg} . T shows a broad maximum for $0.2 \le K_{bg} \le 0.4$ and smallest probabilities 530 531 for very high and very low values of K_{bg} . The biological tracers (lower panel in Fig. 5) are all 532 sensitive to variations in K_{bg} , in particular AOU, DIC, and P* which are 5-10 times more likely 533 for low then high K_{bg} . ALK and PO_4 show maxima for K_{bg} around 0.15-0.2. 534 535 3.5. Probabilities From the 1D Method 536 Figure 6 shows PDFs for the same variables but using the 1D method. The most obvious 537 difference is that the 1D PDFs are much sharper than those obtained with the 3D method. This 538 might be counterintuitive, since information was lost by aggregating the data from 3D to 1D (we discuss this effect further below). The 1D method yields maxima for all tracers for $K_{bg} \le 0.2$. 539 Probabilities for $K_{bg} > 0.4$ are very small for all tracers. Thus the two statistical methods agree 540 that high K_{bg} models are less consistent with the observations than low K_{bg} models. Both 541 methods also exhibit similar shapes for most tracers. E.g. $\Delta^{14}C$, S, AOU, DIC and P* all have 542 maxima for $K_{bg} < 0.2$, CFC11, ALK and PO_4 show maxima for $0.1 \le K_{bg} \le 0.2$, and T shows a 543 broad maximum for $0.2 \le K_{bg} \le 0.3$. 544 545 546 3.6. Sensitivity Tests 547 We conduct four simple sensitivity analyses of the 3D method to gain some insights into the 548 factors that influence the differences in the posterior PDFs between the 3D and 1D methods 549 (Figure 7). First, we test the assumption of neglecting the error of the observations by setting 550 $\sigma_0 = 0$ and re-estimating the total error σ (Table 1). Comparing the resulting PDFs (blue lines)

with the original PDFs (black lines) shows that this effect is negligible for most tracers. Only

CFC11, $\Delta^{14}C$, and DIC show small differences.

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Second, we calculated the PDFs for 1D (horizontally averaged) data but using the 3D method as described in section 2.4.1 (red solid lines in Fig. 7). The re-estimated errors (Table 1) are much smaller than in the 3D case for all tracers, indicating that the model has considerably more skill in reproducing the horizontally averaged observations than the full 3D distributions. Intuitively it makes sense that due to the limited resolution a model's skill improves with increasing spatial scale. Comparison of the solid black and solid red lines in Figure 7 shows that smaller σ results in sharper PDFs, which for most tracers are now similar to the PDFs from the 1D method (Figure 6). This suggests that the main reason for the sharper PDFs in the 1D method (Figure 6) compared with the 3D method (Figure 5) is the smaller estimated σ .

Third, we evaluate the effects of correcting for spatial autocorrelation. Following *Ricciuto et al.* [2008] we remove the lag-1 autocorrelation (a) from the 1D residuals, R, according to:

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$$\overline{E_i^2} = \overline{\left(R_i(z_k) - aR_i(z_{k-1})\right)^2}.$$
 (9)

As expected from earlier studies [*Ricciuto et al.*, 2008; *Zellner and Tiao*, 1964] this approach to account for the autocorrelation (green lines in Fig. 7) leads to broader PDFs (compared to the red solid lines). Neglecting spatial autocorrelation typically results in overconfident parameter estimates. The fact that the PDFs are quite different emphasizes the importance of properly considering spatial autocorrelation.

Fourth, the PDFs are re-calculated for the 1D data (without subtracting autocorrelation) but using the error estimate from the 3D method with σ_O =0 (red dashed lines in Fig. 7). Thus the difference between the red solid lines and the red dashed lines in Fig. 7 isolates the effect of different estimated σ . The difference between the red dashed lines and the blue lines isolates the effect of the reduced information content in the 1D versus the 3D residuals. For most tracers the PDFs are broader than those in the high σ cases (red solid lines) and more similar to the 3D case (blue lines). This indicates that the most important reason for the difference between the 1D and 3D methods (and the explanation for the sharper PDFs in the 1D method) is the differently estimated σ . It also suggests that spatial aggregation, despite a loss of information, can help to improve the model skill, and as a consequence lead to sharper PDFs. For PO_4 , CFC11, and ALK

585 the red dashed lines deviate substantially from the blue solid lines. This indicates an important 586 loss of information due to the averaging. These tracers might not be suitable for the 1D method. 587 588 3.7. Probabilities for Multiple Tracers 589 590 Each of the tracers examined above contains different information and leads to a different PDF 591 for K_{hg} . Our goal, however, is to produce a single PDF combining the information from all 592 tracers as outlined in sub-section 2.4.1. 593 594 The distribution of each tracer is influenced not only by diapycnal mixing and the large-scale ocean circulation, but also by other processes. Some tracers, such as T, S, CFC11, Δ^{14} C, and 595 DIC, are also influenced by air-sea exchange. Thus, the model errors, and hence the PDF, for T 596 e.g., might be influenced by model biases in ocean-atmosphere heat fluxes, which are controlled 597 598 by radiative fluxes as well as sensible and latent heat fluxes. The PDF for S, on the other hand, is 599 influenced by surface ocean water fluxes, which are determined by evaporation, precipitation and 600 river runoff, and thus by the atmospheric hydrological cycle. Because different physical 601 processes control heat and water fluxes (except for evaporation which influences both) it is 602 unlikely that model errors in heat fluxes are strongly correlated with errors in water fluxes. 603 Similarly, the air-sea fluxes of carbon, radiocarbon and CFCs are presumably rather independent 604 from heat and water fluxes. Thus, considering multiple tracers can possibly average out model 605 errors in individual air-sea fluxes. If the errors in the tracer residuals are independent between 606 tracers, a combined likelihood for all tracers can be calculated by multiplying the likelihoods of 607 the individual tracers as described at the end of section 2.4.1. 608 609 On the other hand, if tracers are not independent, multiplication of the likelihoods would lead to 610 overconfident and possibly biased PDFs. Sinking of particulate organic matter (the soft-tissue 611 biological pump), for instance, influences PO₄, AOU, and DIC and thus errors in those tracers 612 cannot be expected to be independent. An objective way to determine independence between 613 different tracers is to examine correlations between the errors of the residuals. As shown in Table

2, the different tracers are generally not independent. PO₄, AOU, and DIC are clearly related for

615 the reasons mentioned above, but other tracer residuals (such as T and S) are also correlated, for 616 less obvious reasons. 617 618 At this point no method that we are aware of has accounted for the cross-tracer correlation. It is 619 highly desirable to develop such a method in the future. For the time being we calculate PDFs for 620 different combinations of uncorrelated tracers (Figure 8). All combined PDFs show low 621 probability for models with high mixing rates ($K_{bg} > 0.3$). The different tracer combinations do 622 not agree well for the probability of low mixing models. Some show a distinct maximum around 623 0.1-0.2 and considerably lower probabilities for lower K_{bg} , whereas others show high probabilities for the lowest diffusivities. We conclude that the observations put a firm upper limit 624 625 on the diffusivities, whereas no unequivocal lower limit can be determined based on the 626 information we have presented here. 627 628 4. Discussion 629 One issue that has not been addressed here is parameter interactions. Generally model tracer 630 distributions are influenced by more than one parameter, each of which is uncertain. Thus, the 631 results obtained by varying one parameter depend on the values of many other parameters. This 632 is also true in our case, and hence the probabilities for different K_{bg} presented here are tentative 633 and should be regarded as a test of the methodology rather than a definitive result. 634 635 Parameter interactions might be most obvious for tracers affected by biological processes such as 636 PO₄, AOU, P*, DIC and ALK, which are sensitive to ill-constrained biological model parameters. 637 Surface nutrient concentrations and deep ocean AOU, P* and DIC, for instance, all depend 638 strongly on the maximum growth rate of phytoplankton (γ) which determines the efficiency of 639 the biological pump. The vertical alkalinity gradient is controlled by the fixed ratio of calcium 640 carbonate versus particulate organic carbon production ($R_{CaCO3/POC}$). These biological model parameters were tuned for a model version with $K_{bg} = 0.15$ ($\gamma = 0.13$ d⁻¹, $R_{\text{CaCO3/POC}} = 0.03$). Thus 641 642 larger errors for those tracers in models with different K_{bg} can be expected because the biological parameters are unadjusted. Interestingly, though, 3 out of 5 biological tracers prefer K_{bg} =0.05. 643

Models with $K_{bg} > 0.15$ therefore overestimate surface nutrient concentrations because of more

intense advective and diffusive transport of nutrient rich deep waters to the surface. Similarly,

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models with $K_{bg} > 0.15$ underestimate the efficiency of the biological pump and hence the deep ocean AOU and DIC, and overestimate P^* . Thus γ should be increased together with K_{bg} . Faster rates of nutrient input into the euphotic zone, in the strong mixing models, also lead to increased primary and export production [Schmittner et al., 2005b] and higher production of CaCO₃, resulting in overestimated vertical alkalinity gradients. Thus, $R_{\text{CaCO3/POC}}$ should be decreased as K_{bg} is increased. Due to computational constraints we are currently not able to retune the biological parameters for each model version with different K_{bg} . A simple optimization of biological parameters for the model version with $K_{bg} = 0.5$ ($\gamma = 0.2$ d⁻¹, $R_{\text{CaCO3/POC}} = 0.02$) results in a decrease of the errors with respect to the untuned values shown in Figure 3, but the errors are still significantly larger than those of the low K_{bg} models. Thus, the true likelihoods for the biological tracers would presumably increase for model versions with high K_{bg} . It is highly desirable to include these known cross-parameter dependencies in a larger model ensemble in the future. Of course, tracer distributions not affected by biological parameters, such as $\Delta^{14}C$ (radiocarbon in our model is not influenced by biological parameters) and CFCs, do not suffer from this complication. Therefore our conclusion that models with $K_{bg} > 0.3$ cm²/s are increasingly inconsistent with observations holds true based on these tracers alone. An intriguing result is that horizontally averaged data (1D method) lead to sharper PDFs than the full 3D data distribution. We have shown that this is likely due to the improved skill of the model in simulating horizontally averaged observations (smaller σ). This seems to be an advantage of the 1D method. However, horizontal averaging has the obvious disadvantage that major model problems in the horizontal tracer distribution are undetectable. Consider, for example, a model with deep water formation in the North Pacific instead of the North Atlantic. Such a model might still reproduce the horizontally averaged tracer distributions reasonably well, despite the fact that it is obviously wrong. Nevertheless, our results suggest that an optimal degree of spatial aggregation might exist, at which high model skill and the resulting sharp PDFs could be

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combined with 3D spatial information.

Griffies [2000] showed that z-level models, such as the one used here, can exhibit spurious diapycnal mixing due to numerical errors. For a model with the same numerical scheme as that used here (the second order accurate, flux corrected transport scheme, FCT) and a resolution of $2.4^{\circ} \times 2.4^{\circ}$ they found large spurious mixing in the order of $0.3 \text{ cm}^2/\text{s}$, whereas for a model with $1.2^{\circ} \times 1.2^{\circ}$ the spurious mixing was negligible due to the improved resolution of the western boundary currents. Our zonal grid resolution (which is more important than the meridional resolution for simulating western boundary currents) of 1.8° is in between those reported by *Griffies* [2000]. Thus, we cannot exclude the possibility that our model exhibits spurious mixing, particularly for the low K_{bg} cases. However, we can exclude the possibility that the model is dominated by numerical diffusion, because in this case changing the explicit diffusivity would not alter the solution. By contrast, in our experiments, the circulation is significantly different between all runs, including those with low diffusivity. The maximum overturning at 25°N in the Atlantic in the unperturbed pre-industrial model spinup, for example, is 10.8 Sv, for $K_{bg} = 0.01$, 12.2 Sv in the $K_{bg} = 0.05 \text{ case}$, and 13.8 Sv for $K_{bg} = 0.1$.

An outstanding question remains as to how to interpret the range spanned by the C⁴MIP model results. This question can be addressed only by a systematic and probabilistic comparison with observations that sample the relevant parametric and structural uncertainties. Our study represents a step towards this goal, though here we have sampled only a small fraction of the full range of parametric uncertainty. We have shown that low values of K_{ν} are most consistent with ocean tracer observations, and that most of the C⁴MIP models fall within the range of ocean carbon uptake simulated by varying K_{be} values in this study. If the values for K_{v} were known for the different C⁴MIP models, it would be possible to reject projections from models with high K_{ν} values, or to judge them as less reliable than those from models with low K_{ν} . However, we are not aware of a published documentation of the values of K_{ν} used by the C⁴MIP models (effective diapycnal diffusivity can also contain a difficult-to-evaluate numerical component). There is an additional complication arising from different structural types of ocean models represented in C⁴MIP (box models, versus 2D models, versus GCMs). In practice, therefore, it remains difficult to assign the likelihoods we have derived here directly to the C⁴MIP model projections. However, we think that the methodology developed here can be used for multi-model assessments in the future, given that spatially resolved tracer model data output is provided.

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5. Conclusions

709 We have shown that uncertainties in the value of diapycnal mixing in the pelagic ocean 710 contribute to the spread in future model projections of CO₂ and climate in response to 711 anthropogenic carbon emissions. Models with low mixing lead to slower uptake of carbon and 712 heat by the ocean, therefore contributing to higher atmospheric CO₂ and warmer air 713 temperatures. These results suggest that models with large ocean vertical mixing (high K_{ν}) 714 systematically underestimate future warming and CO₂ concentrations, and that the range in 715 vertical mixing between models is a contributing factor to the large ranges in transient climate 716 sensitivity and climate-carbon cycle feedbacks that have been diagnosed in earlier model 717 intercomparisons. 718 719 Globally averaged metrics such as historic changes in globally averaged surface air temperature 720 or ocean heat content do not provide strong constraints on the vertical diffusivity [Tomassini et 721 al., 2007]. We show that spatially resolved physical, geochemical and biogeochemical tracer 722 observations in the ocean can be used to reduce the uncertainty of this parameter (and, by 723 extension, that of future climate projections). These observations provide a firm upper limit on 724 the value of K_{hg} , whereas the lower limit is less well constrained. Our best estimate for the background diapycnal diffusivity in the pelagic ocean is 0.05-0.2 cm²/s, in agreement with 725 726 independent estimates based on dye dispersion experiments and microstructure turbulence 727 measurements [Ledwell et al., 1993; Toole et al., 1994]. 728 729 We have developed a Bayesian model-data fusion method that can be used to quantify and 730 reduce the uncertainty in future climate-carbon cycle projections. Remaining issues left for 731 future work include (i) cross-tracer correlations, (ii) parameter interactions, and (iii) the optimal 732 degree of spatial aggregation. Resolution of the second issue is simply one of computational 733 resources, while the first needs further development and refinement of the existing statistical 734 methodology and theory. To resolve the third issue, the optimal degree of aggregation can 735 presumably be determined in a sensitivity study with successively larger spatial scales of 736 averaging. None of those issues seem insurmountable. The prospect of robust likelihood-based 737 model assessment, using multiple observations considering spatial and temporal autocorrelation

738 as well as cross-tracer correlations has the potential to lead towards truly probabilistic climate-739 carbon cycle projections. 740 741 Acknowledgements 742 We thank Roman Tonkonojenkov, Bob Key, Katrin Meissner, Murali Haran, Sham Bhat, Marlos 743 Goes, Josh Dorin, and Brian Tuttle for helpful discussions. Any potential errors and omissions 744 are, of course, ours. We are grateful for the support of Michael Eby and Andrew Weaver from 745 the University of Victoria model development team. Financial support from the National 746 Science Foundation, the Canadian Foundation for Climate and Atmospheric Sciences, and the 747 Penn State Center for Climate Risk Management is gratefully acknowledged. Any opinions, 748 findings and conclusions or recommendations expressed in this material are those of the authors 749 and do not necessarily reflect the views of the funding entity. 750

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903 Figure captions 904 905 Figure 1. Hindcasts and projections of atmospheric CO₂ concentration (top) and near surface air 906 temperature (SAT) anomalies from the 1960-1990 levels (bottom) for model versions with 907 different values of K_{bg} . The emission scenario (SRES A2 until year 2100 and linear decrease 908 until year 2300 afterwards) is shown as the heavy dotted line in the top panel with the scale in 909 the bottom right corner ranging from 0-30 Gt C / yr. For reference: current (2007) levels are 910 about 8.5 Gt C / yr [Canadell et al., 2008]. The insets in the upper left region of each panel show 911 a zoom into the hindcast period (1800-2007) including CO₂ observations from Mauna Loa 912 [Keeling and Whorf, 2005] and ice cores [Neftel et al., 1994] (circles) and temperature 913 observations from the HadCRUT3 [Brohan et al., 2006] dataset (black noisy line). 914 915 Figure 2. Upper ocean (0-700 m) heat content changes (from year 1961) as simulated by the 916 different model versions (lines) compared to observations (grey shading) from *Domingues et al.* 917 [2008]. The dark grey shading denotes nine year running mean values for comparison with 918 decadal averages plotted for the model simulations. The light gray shading shows three-year 919 averages. 920 921 Figure 3. Effects of reduced ocean heat and carbon uptake on projected warming resulting from 922 smaller vertical mixing. The solid line shows the global mean surface air temperature anomaly for a run with low vertical mixing (K_{bg} =0.1) minus that from a run with high vertical mixing 923 $(K_{bg}=0.5)$, including both effects, reduced heat and reduced carbon uptake. The dashed line 924 925 shows the effect of reduced heat uptake alone from a sensitivity experiment with K_{bg} =0.1 in which atmospheric CO₂ evolution is prescribed to be identical to that from the K_{bg} =0.5 926 927 simulation. The effect of reduced carbon uptake shows as the difference between the dashed and 928 solid lines. 929 930 **Figure 4.** Normalized RMS errors E (left), E' (center) and correlation coefficients r (right) for 931 3D distributions of different physical (top) and biogeochemical (bottom) tracers as a function of 932 the diapycnal background diffusivity K_{bg} .

934 **Figure 5.** Posterior PDFs using the 3D method (eq. 3) for different physical (top) and 935 biogeochemical (bottom) tracers as a function of the diapycnal background diffusivity $K_{b\sigma}$. 936 937 Figure 6. Posterior PDFs using the 1D method (eq. 7) for different physical (top) and 938 biogeochemical (bottom) tracers as a function of the diapycnal background diffusivity $K_{b\sigma}$. 939 940 Figure 7. Sensitivity tests. Posterior PDFs as a function of the diapycnal background diffusivity K_{bg} for different tracers using the 3D method, but different assumptions in the statistical analysis 941 942 as described in the text. Black lines show the full 3D method and are identical to the PDFs 943 shown in Figure 5. Blue lines neglect the error in the observations (σ_0 =0). Note that for many 944 tracers the black lines are indistinguishable from and covered by the blue lines. Solid red lines 945 use the 3D method as described in subsection 2.4.1 but use horizontally averaged 1D data. Note 946 that the error estimate (σ) is strongly reduced (see also Table 1) and that the PDFs are much 947 sharper compared to the un-averaged 3D data (black lines). Red dashed lines also use the 3D 948 method and horizontally averaged 1D data but instead of estimating the error (as done for the 949 solid red lines) the error estimate from the 3D data (black lines) is used. Thus the difference 950 between the red solid and red dashed lines are only due to different σ . Green lines compared to 951 the red solid lines illustrate the broadening effect on the PDFs from removing the spatial 952 autocorrelation using eq. (9). 953 Figure 8. Posterior PDFs as a function of the diapycnal background diffusivity K_{bg} for different 954 955 combinations of uncorrelated (see Table 2) tracer distributions using the 3D method. Compared 956 with the PDFs of the individual tracers as shown in Figure 5, the combined PDFs are much 957 sharper illustrating the power of using multiple tracers to constrain model parameters. 958

Table 1. Estimated model error σ_M for different assumptions and tracers as calculated from the K_{bg} =0.15 case.

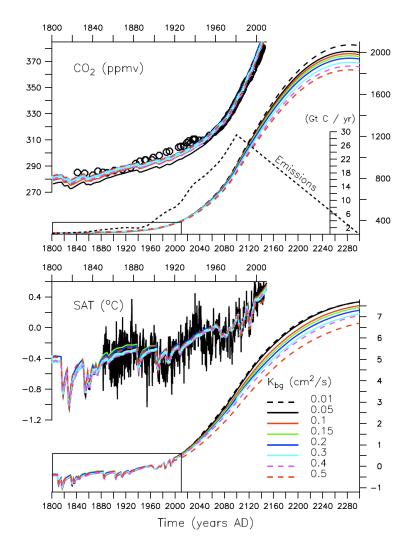
| | | T | S | $\Delta^{14}C$ | CFC11 | PO_4 | AOU | DIC | ALK | P^* |
|----|-------------------|------|-------|----------------|-------|-----------|------|-----------|-----------|-----------|
| | | (K) | | (permil) | (pM) | (μM) | (mM) | (μM) | (μM) | (μM) |
| 3D | $\sigma_O \neq 0$ | 0.90 | 0.18 | 0.0 | 0.24 | 0.20 | 25 | 19 | 13 | 0.16 |
| | | | | 20 | | | | | | |
| 1D | $\sigma_{O}=0$ | 0.24 | 0.079 | 5.9 | 0.053 | 0.064 | 3.7 | 9.0 | 6.6 | 0.062 |

Table 2. Cross-tracer error correlation for the 3D method in the model with K_{bg} =0.15 cm²/s.

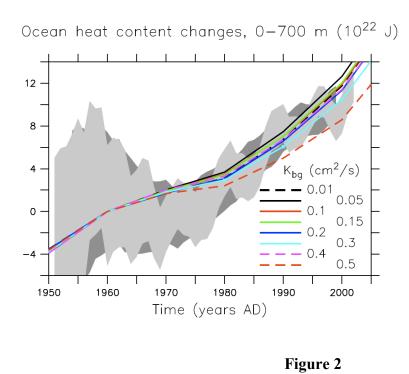
Absolute values larger than 0.3 are shown in bold.

| | T | S | $\Delta^{14}C$ | CFC11 | PO_4 | AOU | DIC | ALK |
|----------------|-------|-------|----------------|-------|--------|-------|-------|-------|
| T | | | | | | | | |
| S | 0.48 | | | | | | | |
| $\Delta^{14}C$ | 0.26 | 0.03 | | | | | | |
| CFC11 | 0.01 | -0.04 | 0.39 | | | | | |
| PO_4 | -0.42 | -0.22 | -0.41 | -0.23 | | | | |
| AOU | -0.09 | 0.12 | -0.36 | -0.40 | 0.65 | | | |
| DIC | -0.20 | 0.31 | 0.33 | -0.13 | 0.52 | 0.76 | | |
| ALK | 0.04 | 0.54 | 0.23 | -0.07 | 0.12 | 0.42 | 0.72 | |
| P^* | -0.44 | -0.42 | -0.19 | 0.08 | 0.69 | -0.08 | -0.05 | -0.23 |

968969 Figures



974 Figure 1



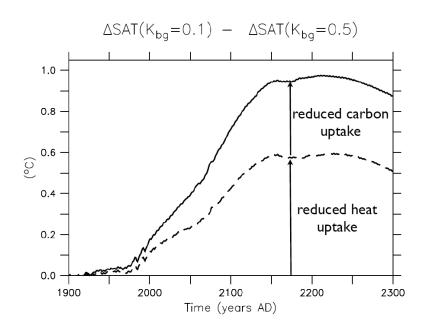
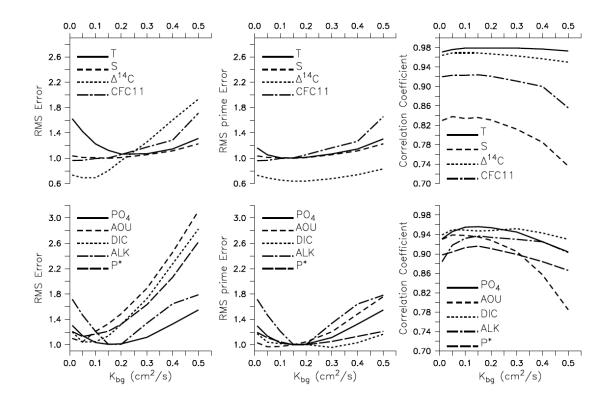


Figure 3



988 Figure 4

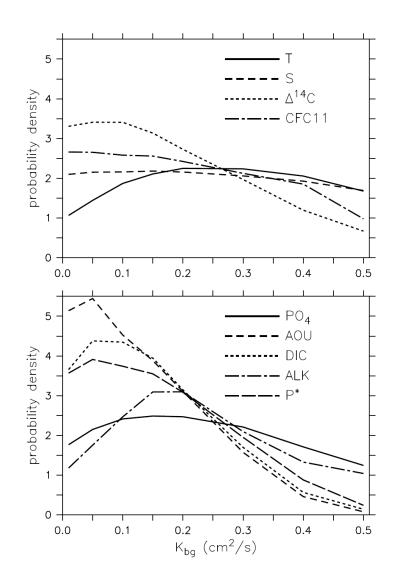


Figure 5

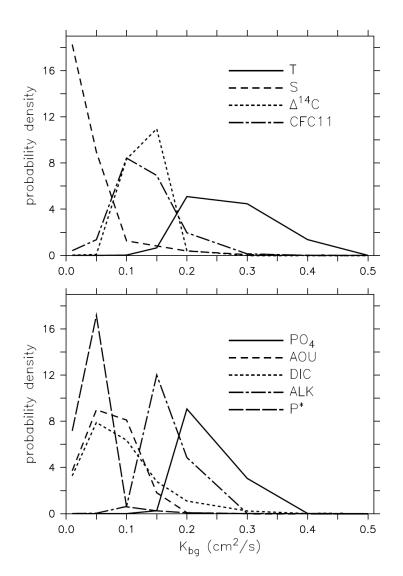
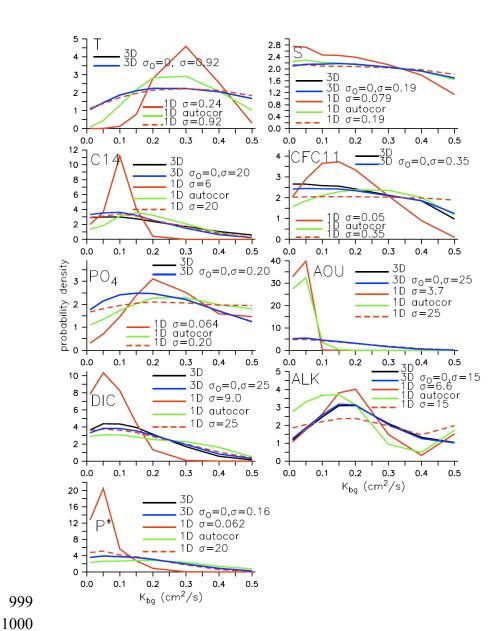


Figure 6



1002 Figure 7

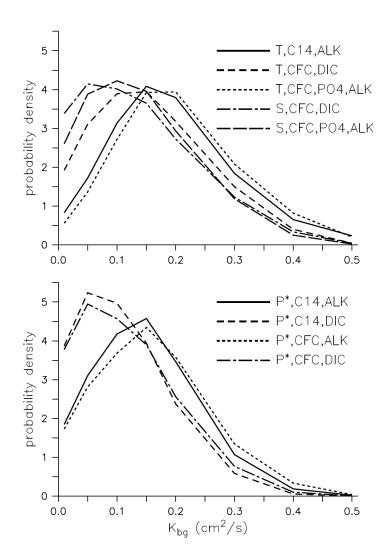


Figure 8